

Exercise 1

1)

$$\bar{I}_a = \frac{\bar{V}_a}{Z_{eq}}$$

$$Z_L = j3 \Omega \quad R_1 = 18 \Omega \quad R_2 = 12 \Omega$$

$$\bar{V}_a = \frac{346}{\sqrt{3}} \angle 0^\circ V = 199,76 \angle 0^\circ V$$

$$Z_{eq} = Z_L + \left(R_2 \parallel \frac{R_1}{3} \right) = j3 + \frac{(12) \left(\frac{18}{3} \right)}{12 + \frac{18}{3}} = 4 + j3$$

$$= 5 \angle 36,87^\circ \Omega$$

$$\bar{I}_a = \frac{199,76 \angle 0^\circ}{5 \angle 36,87^\circ} = 39,95 \angle -36,87^\circ A$$

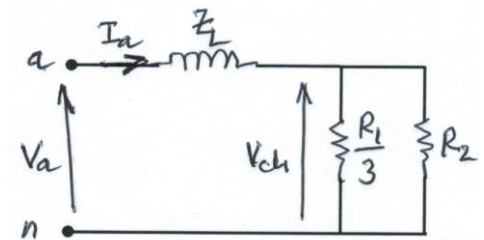


Schéma monophasé équivalent

$$2) \quad \bar{S} = 3 \bar{V}_a \bar{I}_a^* = 3 \times 199,76 \times (39,95 \angle -36,87^\circ)^* = 23942 \angle 36,87^\circ = 19154 + j14365 VA$$

donc $P = 19154 W$ et $Q = 14365 Var$

$$3) \quad \bar{V}_{ch} = \bar{V}_a - Z_L \bar{I}_a = 199,76 - (j3)(39,95 \angle -36,87^\circ) = 159,81 \angle -36,87^\circ V$$

donc $U_{ch} = V_{ch} \sqrt{3} = 159,81 \sqrt{3} = 276,8 V$

Exercise 2

$$1) \quad Z = z_l = (0,1 + j0,5) \times 100 = 10 + j50 = 51 \angle 78,69^\circ \Omega$$

$$Y = y_l = j6 \cdot 10^{-6} \times 100 = j0,6 \times 10^{-3} S$$

$$A = 1 + \frac{YZ}{2} = 1 + \frac{j0,6 \times 10^{-3} (10 + j50)}{2} = 0,985 + j3 \cdot 10^{-3} = 0,985 \angle 0,17^\circ$$

$$B = Z = 51 \angle 78,69^\circ \Omega$$

2)

$$\bar{V}_R = \frac{U_R}{\sqrt{3}} = \frac{132}{\sqrt{3}} = 76,2 \angle 0^\circ kV$$

$$I_R = \frac{S_R}{\sqrt{3} U_R} = \frac{125 \cdot 10^6}{\sqrt{3} \times 132 \cdot 10^3} = 546,7 A$$

$$\arccos(0,9) = 25,84^\circ \rightarrow \bar{I}_R = 546,7 \angle -25,84^\circ A$$

$$\bar{V}_s = A \cdot \bar{V}_R + B \cdot \bar{I}_R = (0,985 \angle 0,17^\circ)(76,2 \angle 0^\circ) + (51 \angle 78,69^\circ)(546,7 \times 10^{-3} \angle -25,84^\circ)$$

$$= 91,9 + j22,45 = 94,6 \angle 13,73^\circ kV$$

$$U_s = \sqrt{3} V_s = \sqrt{3} \cdot 94,6 = 163,8 kV$$

3)

$$V_{R0} = \frac{V_s}{|A|} = \frac{94,6}{0,985} = 96,04 kV$$

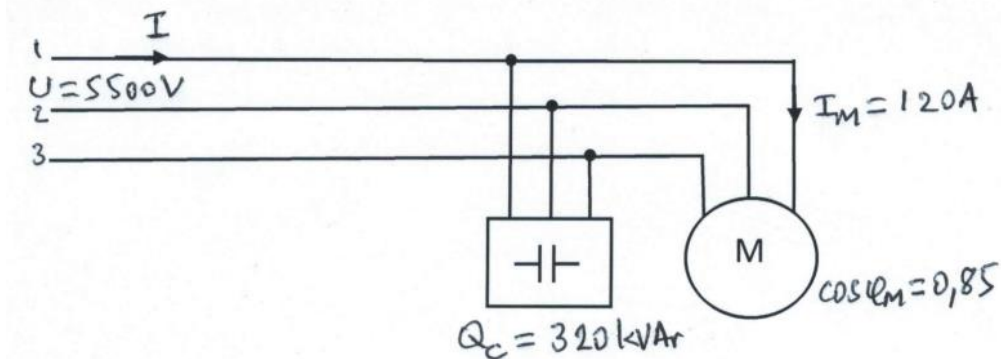
$$RV = \frac{V_{R0} - V_R}{V_R} = \frac{96,04 - 76,2}{76,2} = 0,26 = 26\%$$

ou

$$RV = \frac{V_s - |A| V_R}{|A| V_R} \times 100 = \frac{94,6 - 0,985 \times 76,2}{0,985 \times 76,2} \times 100 = 26\%$$

Exercise 3

1)

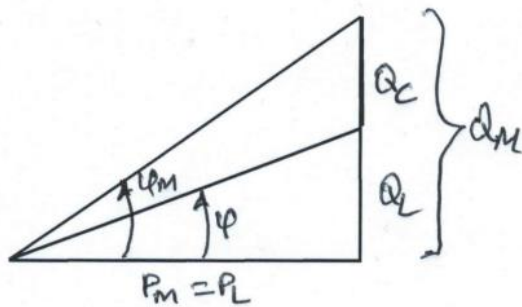


2) $S_M = \sqrt{3}UI_M = \sqrt{3} \times 5500 \times 120 = 1143,2 \text{ kVA}$

$P_M = S_M \cdot \cos \varphi_M = 1143,2 \times 0,85 = 971,7 \text{ kW}$

$Q_M = S_M \cdot \sin \varphi_M = 1143,2 \times \sin(\arccos(0,85)) = 602,2 \text{ kVar}$

3)



5) $P_L = P_M$

$S_L = \sqrt{P_L^2 + Q_L^2} = \sqrt{971,7^2 + 282,2^2}$
 $= 1011,8 \text{ kVA}$

$\cos \varphi = \frac{P_L}{S_L} = \frac{971,7}{1011,8} = 0,96$

$I = \frac{S_L}{\sqrt{3}U} = \frac{1011,8 \cdot 10^3}{\sqrt{3} \times 5500} = 106,2 \text{ A}$

4)

$Q_L = Q_M - Q_C$
 $= 602,2 - 320 = 282,2 \text{ kVar}$